

Electrical and electromagnetic properties of isolated carbon nanotubes and carbon nanotube-based composites

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ABSTRACT

Isolated carbon nanotubes (CNTs), CNT films and CNT-polymer nanocomposites are a new generation of materials with outstanding mechanical, thermal, electrical and electromagnetic properties. The main objective of this article is to provide a comprehensive review on the investigations performed in the field of characterizing electrical and electromagnetic properties of isolated CNTs and CNT-reinforced polymers either theoretically or experimentally. The results reported in literature are reviewed and evaluated based on employed and/or developed methods by focusing on the electrical conductivity, permittivity and permeability properties. Available analytical and numerical simulations for predicting electrical properties of CNT-based composites are also reviewed. Besides, equivalent circuit modeling of nanocomposites containing CNTs is presented. The influence of effective parameters on overall electrical and electromagnetic characteristics of CNT-reinforced polymers is discussed based on published data. Therefore, highlighting the recent trends and challenges engaged in new investigations, those aspects which are required to be more deeply explored are introduced. **Polyolefins J (2017) 4: 43-68**

Keywords: Carbon nanotubes; nanocomposite; electrical properties; permittivity; permeability.

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INTRODUCTION

Carbon nanotubes (CNTs) as a new generation of materials have unique mechanical, thermal, electrical and electromagnetic properties [1-6]. Carbon nanotubes in semiconducting (zigzag) and metallic (armchair) types are considered as promising reinforcements for improving the properties of polymers. By incorporating CNTs into polymers, new category of nanocomposites with improved properties can be achieved not only from mechanical point of view but also from electrical and electromagnetic aspects.

The main objective of this article is to review the researches that conducted on the field of electrical and/or electromagnetic properties of CNT-reinforced polymers through analyzing electrical conductivity, permittivity and permeability of CNT-based films and composites. These parameters have a direct influence on determining the key parameters such as reflection and transmission coefficients of microwave [7], loss tangent [8] and skin depth [9]. They are important especially in high-frequency applications. Since simulation techniques including molecular dynamic (MD), Brownian dynamics (BD) and electrical circuit modeling approach are a challenging task to characterize the electrical behavior of CNT-based composites, experimental methods have been widely used by researchers [10-14].

Electrical properties of carbon nanotube can be exploited in various applications like display devices [15], batteries [16], fuel cells [17], super capacitors [18], solar cells [19] and transistors [20]. Due to their outstanding electromagnetic properties, they are also employed for constructing microwave lenses, waveguide and antennas [21], electromagnetic shielding [4-6, 22-27] and microwave absorption films [28,29,26]. Consequently, correct understanding of their functionality in electric and electromagnetic fields plays an important role in their development steps for their future potential applications.

In this article, first of all, the morphology and nanostructure of CNTs are explained and then the basic framework of electromagnetic properties is outlined. Different theoretical modeling and simulation methods for extracting electrical properties of individual CNTs and CNT-reinforced polymers are introduced

afterward. Experimental measurements reported in the literature are reviewed and the trend of results is discussed by focusing on the electrical conductivity, permittivity and permeability properties.

CNT AND CNT-BASED COMPOSITES

A carbon nanotube (CNT) can be schematically considered as a rolled graphene sheet with a hexagonal lattice structure consisting of carbon atoms. In carbon nanotubes, each carbon atom is connected by covalent bonds to three other adjacent carbon atoms. Some researchers reported that the outermost wall of a MWCNT is responsible for its electrical conductivity. But recently it is reported that all walls contribute to the electrical properties of MWCNT [30,31]. MWCNTs always show metallic behavior and have diameters between several nanometers to tens of nanometers and their lengths are larger than 100 nm [32], but SWCNTs can show either metallic (Figure 1, B (right)) or semiconducting (Figure 1, B (left)) behavior according to their chirality (Figure 1, A) [33].

New generation of nanocomposites is created by incorporation of CNTs into polymeric matrices. Both thermosetting and thermoplastic resins are used for this purpose. Thermoplastic polymers include polypropylene, polystyrene, polyethylene, poly (methyl methacrylate), polycarbonate and nylon. Thermosetting polymers include polyester, vinyl ester, epoxy, phenolic, polyimide, polyurethane and silicone. Also polymers in terms of electrical properties are divided into two kinds of conductive and insulator polymers. Carbon nanotubes are employed to improve the electrical properties of insulating polymers such as PU, PEMA, PMMA, PC, epoxy, vinyl ester, PS, PVA,

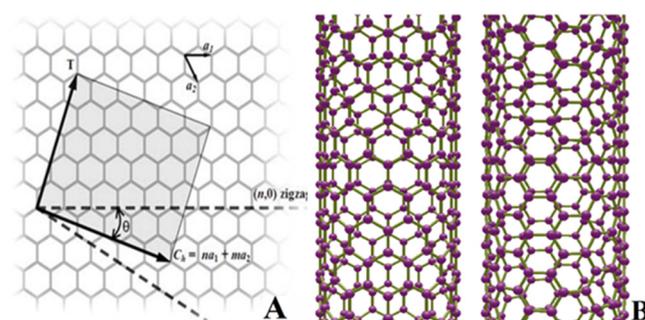


Figure 1. (A) Chirality vector of carbon nanotubes, (B) Armchair structure (6, 6) and Zigzag (12, 0) respectively, from right to left [33].

PCL, PI or even conductive polymers such as PANI, PPY, PEDOT-PSS.

ELECTROMAGNETIC AND ELECTRICAL PARAMETERS

Those characteristic parameters defining electrical and electromagnetic properties of a material are briefly explain in this section.

Electrical conductivity

Electrical conductivity is a parameter showing ability of passing the electrical current through the material. Electrical conductivity is formed in two forms, direct current (without frequency-dependent sources) and alternating current (dependent to frequency). Microwave electrical conductivity is calculated using the permittivity according to equation 1:

$$\sigma_{mw} = 2\pi f \epsilon_0 \epsilon'' \quad (1)$$

where σ_{mw} is the electric conductivity (S/m), f is the frequency (Hz), ϵ_0 is the vacuum permittivity ($\epsilon_0 = 8.854 \times 10^{-12}$ F/m) and ϵ'' is the imaginary permittivity. Microwave electrical conductivity (σ_{mw}) which is sum of the direct current (DC) and alternating current (AC) is expressed by equation 2:

$$\sigma_{mw} = \sigma_{ac} + \sigma_{dc} \quad (2)$$

By using dielectric relaxation spectroscopy (DRS) technique the response of the system is taken through placing the samples between two capacitor plates and the applying alternating voltage [34]. By measuring complex impedance $Z^* = Z' - iZ''$, complex permittivity can be obtained according to equation 3 [35]:

$$\epsilon^*(\omega) = \frac{1}{i\omega Z^*(\omega)C_0} \quad (3)$$

Where ($\omega=2\pi f$) is the angular frequency and C_0 is the equivalent capacitance of the free space [14].

With increasing CNT content in a polymer matrix, a sharp rise in conductivity of nanocomposite is observed at a specific CNT content. This is known as percolation, implying on formation of a 3Delectrically conducting network within the polymer matrix. The percolation threshold can be calculated by plotting

the electrical conductivity versus the volume fraction of CNTs and fitting with a power law function [36,10,11], $\sigma = \sigma_0(\nu - \nu_0)^\beta$, where σ is the electrical conductivity of the composite, σ_0 is the specific conductivity, ν is the volume fraction of CNTs, ν_0 is the volume fraction at the percolation threshold and β is a parameter related to the system dimensionality.

Although the lowest percolation thresholds in the CNT-based composites have been almost obtained by using the solution method [23], the percolation threshold achieved by in-situ polymerization method is about 0.0025 [11].

Permittivity

Complex permittivity (ϵ) is defined as the product of the relative permittivity multiplied by the vacuum permittivity constant ($\epsilon_0 = 8.85 \times 10^{-12}$ F/m). In equation 4, ϵ , D and E are the electric permittivity, electric flux density (q/m^2) and electric field intensity (v/m), respectively.

$$D = \epsilon E \quad (4)$$

Complex relative permittivity (ϵ_r) consists of two real and imaginary parts. The real part (ϵ') is known as dielectric constant or charge storage and the imaginary part (ϵ'') is known as dielectric losses or loss factor ($\epsilon_r = \epsilon' - j\epsilon''$). The imaginary part indicates the ability of material in absorption of radio frequency waves. So, high value of this parameter (loss factor), indicates materials with high absorption properties.

Permittivity at the megahertz-range frequency has high values [7] and at the gigahertz-range frequency is greatly reduced [8]. In general, permittivity always decreases by increasing the frequency. This performance occurs at high CNT volume fractions. It was shown that the real and imaginary parts of the electrical conductivity affect this parameter. Finally, for nanocomposites with higher electrical properties, the lower permittivity, especially in its imaginary part is required.

Permeability

The complex permeability (μ), as shown in equation 5, is expressed as the product of the relative permeability (μ_r) multiplied by the vacuum permeability

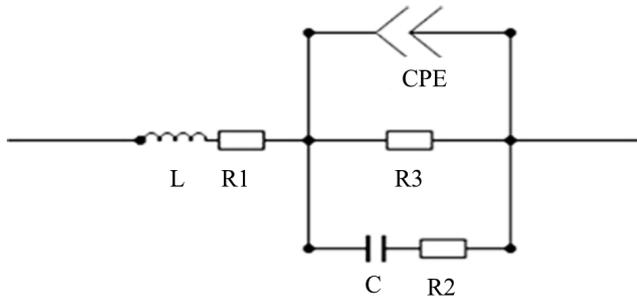


Figure 2. The equivalent circuit model of the t-MWCNT/EP and m-MWCNT/EP composites [54].

($\mu_0 = 4\pi \times 10^{-7} \text{H/m}$). Complex relative permeability (μ_r) consists of two real and imaginary parts. The real part (μ') is known as magnetic storage and the imaginary part (μ'') is known as magnetic loss ($\mu_r = \mu' - j\mu''$).

$$B = \mu H \quad (5)$$

where, B is the magnetic flux density (Tesla) and H is the electric field intensity (A/m).

For enhancing microwave absorption, the initial permeability (μ_i) of the absorbing material should address the highest possible value. For example, the μ_i of ferromagnetic materials could be expressed as $\mu_i = \frac{M_s^2}{akH_cMS + b\lambda\xi}$, where a and b are constants obtained by the material compositions, λ is the magnetostriction constant, ξ is the elastic strain characteristic of the crystal, and k is a proportionality coefficient. As it can be seen, the permeability can be enhanced either by improving M_s or by decreasing H_c . This is favorable for enhancing the microwave absorption capability of the material [37].

Loss tangent

Loss tangent, known as dielectric loss or $\tan \delta$, is described by equation 6; this parameter represents the ability of converting the stored energy in the material to heat energy. High loss factor (ϵ'') and high loss tangent ($\tan \delta$) show high ability of the materials in absorbing the radio waves [38].

$$\tan \delta = \frac{\epsilon''}{\epsilon'} = \sigma \epsilon_0 \epsilon_r \quad (6)$$

Materials with $\tan(\delta) \gg 1$ are known as good conductors, and with $\tan(\delta) \ll 1$ are known as poor conductors [39].

When the electromagnetic radiation encounters with a conductor/insulator composite surface, the electric field produces two different electric currents (conduction current and displacement current) in the material. These currents increase the loss factor (imaginary part of the permittivity). In general, absorbing the electromagnetic radiations and converting these waves into heat, depends on the complex relative permittivity and loss tangent [40]. The loss tangent or dielectric loss factor increases in CNT-based composites by increasing the diameter and volume fraction of CNT.

Skin depth

The skin depth is a distance evaluating ability of the electromagnetic field to propagate within a material [41]. From theoretical point of view, a good conductor has zero skin depth. While for aluminum, this distance is placed between 0.748 to 0.611 μ_m for the Ku frequency band (12 to 18 GHz) at $\mu_r = 1$ and resistivity of $2.65 \times 10^{-8} (\Omega m)$. Skin depth is calculated using below equation:

$$\delta = \sqrt{\frac{2}{\omega \mu \sigma}} = \sqrt{\frac{2}{\pi f \mu}} \quad (7)$$

where ρ is the resistivity of the conductor in $\Omega.m$, f is the frequency in Hz and μ is the absolute magnetic permeability of the conductor.

THEORETICAL METHODS OF OBTAINING ELECTRICAL PROPERTIES OF ISOLATED CNTs AND NANOCOMPOSITES CONTAINING CNTs

In a general classification, the electrical properties have been extracted by both the theoretical and experimental methods. In this section, the theoretical methods categorized under simulations and modeling techniques are introduced.

Molecular dynamics simulations (MD)

In molecular dynamics simulations (MD) and Brownian dynamics simulations (BD), the simulation of carbon-carbon bonds of one or several carbon nanotubes is explained. Although these methods are very accurate in prediction, they are suffering from complex formulations, intensive computations and considerable simulation runtimes. They are able only to compute the limited lengths of carbon nanotubes [42].

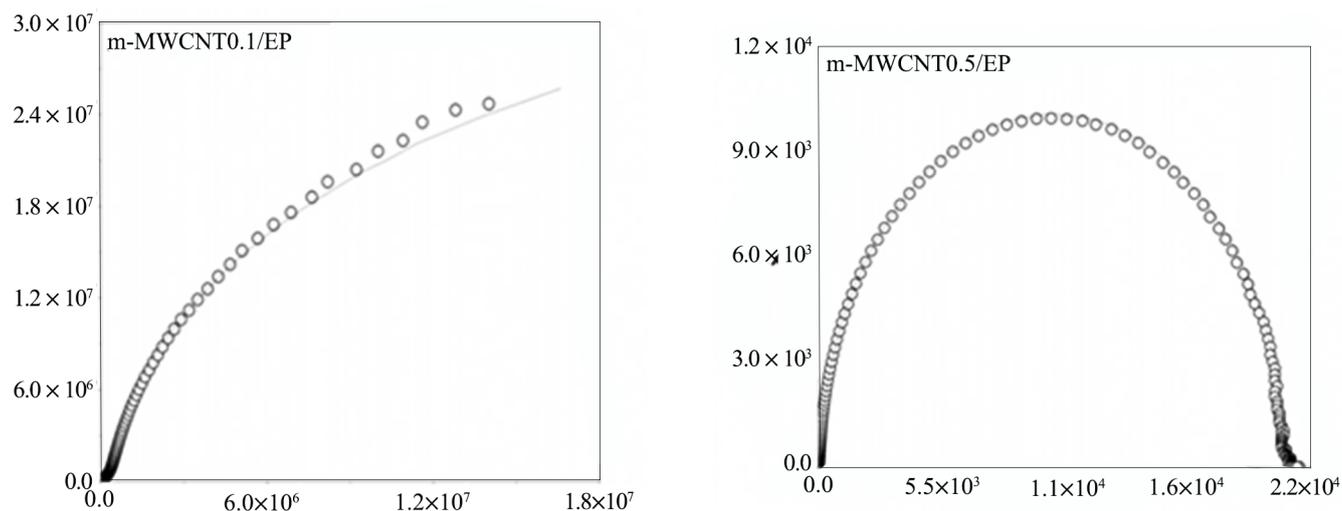


Figure 3. Impedance Nyquist plot for nanocomposites with 0.1 vol% (left) and 0.4 vol% (right) of CNT [54].

This limitation avoids to simulate the nanocomposites and ultimately their properties with broader perspectives. As it is observed in Table 4, in most of the simulation methods, the physical (mechanical) properties have been studied.

MODELING

Modeling methods are divided into three categories as: modeling of interconnections of CNTs, modeling of nanocomposites containing CNTs and probabilistic methods.

Modeling of interconnections of CNTs

In the approach of modeling of interconnections of CNTs, the models have been obtained based on existed theories for making the models. In this type of modeling, the primary data and design assumptions are extracted from MD simulation. For instance, parameters such as mean free path (MFP) (which is considered as 1.6 μm in this type of modeling) and also the van der Waals gap between shells (which is equal to 0.34 nm in modeling) are extracted from MD simulation. Although the accuracy of the modeling methods is lower than that of the MD simulation, they are not limited to small systems and through presenting some proofs and assumptions all types of single, double and multi-walled CNTs and also bundle of CNTs can be modeled.

In all contents related to polymer-based nanocomposites, the data have been collected based on the re-

sults extracted from tests on different combinations. Burke studied on the electrical properties of nanotubes at high frequency by extracting the electrical equivalent circuit of single wall carbon nanotubes [43, 44]. Within the recent decade, considering the simple structure of single wall carbon nanotubes comparing to double and multiwall ones, these types of carbon nanotubes have received more attentions. Considerable advancements in this context ultimately resulted in accessing to functional specifications of a single wall carbon nanotube and bundle of single wall carbon nanotubes [44, 45]. For instance, researches have been performed to establish equivalent circuit of a SWCNT [44, 46] and ultimately resulted in functional predictions of SWCNT connections [44]. In some papers, the dependence of nanotubes diameter for connection and Ohmic resistances of a bundle of SWCNT which are very important for implementation of nanotubes connections, have been evaluated [47]. The maximum value of conductive channel per cross-section area is required to reach the maximum conductivity in the applications of CNTs interconnections. Naeemi and Meindl [45] examined and calculated the number of conductive channels available in MWCNT by the approximate method and also presented a physical model of MWCNT.

Higher diameters of MWCNTs will be led to higher electrical performance [46, 47]. Puet al. [48] have constructed the electrical model of DWCNT interconnections. DWCNTs have a simpler structure than

MWCNTs, because the van der Waals force within the gap between two shells remains in the constant value. In DWCNTs, the diameter of internal shell is different from that of external shell; therefore their resistances will be different from each other.

The recent tests show that the resistance of a MWCNT [49] or bundle of MWCNTs [50] may be lower than that of an ideal conductor SWCNT, and also it is evident that more than one wall is effective in defining their conductivity.

Electrical conductivity of a CNT is described by equation 8:

$$G = G_0 = (2e^2/h)M \quad (8)$$

In the above equation, $G_0 = (2e^2/h) = (12.9k\Omega)^{-1}$, e is the electron charge; h is Planck's constant and M is the number of available conductive channels.

Electrical conductivity and resistance of all types of CNTs which have been obtained using theoretical modeling are tabulated in Table 1 [51-53].

Modeling of nanocomposites containing CNTs

The second category of modeling that is known as semi-empirical modeling is dealing with modeling of all types of nanocomposites containing CNTs. Electrochemical impedance spectroscopy (EIS) is an analytical method for investigating the properties of numerous complex nonlinear electrochemical processes with different conditions (such as temperature, pressure, etc.) that uses relatively simple equivalent circuits (consist of resistance, inductor and capacitor). Ultimately, upon drawing the Nyquist impedance diagram and extraction of corresponding data, the respective electrical model will be extracted.

Cheng et al. [54] presented an electrical equivalent circuit model of nanocomposites containing MWCNT and epoxy with use of semi-empirical method shown in Figure 2.

Results proved that the simulated impedance spectra of the equivalent circuit (see Figure 2) fitted the actual impedance spectra of composites (Figure 3). Then Figure 2 could be confirmed as the equivalent circuit model of the composites prepared herein. Specifically, the equivalent circuit consists of a capacitance (C),

an inductance (L), a constant phase element (CPE) and three resistances (R1, R2, and R3). Because the t-MWCNT/EP and m-MWCNT/EP composites have similar microstructures, so they have similar equivalent circuit elements [54].

The corresponding parameters from the equivalent circuit model have been calculated and shown in Table 2.

The impedance Nyquist plot obtained from EIS includes a circular part and an inclined line. This type of plot (plot with one time constant) is simulated by the simple electrical circuits. In Figure 4, the impedance Nyquist plots are shown for the specimens containing 0.1 and 3 wt% of MWCNT [55].

The electrical equivalent circuit extracted from the impedance plots is depicted in Figure 5. This equivalent circuit comprises of four electrical elements including solution resistance, charge transfer resistance, double-layer capacitance and Warburg impedance.

The numerical values of electrical equivalent circuit elements presented for the investigated nanocomposites are presented in Table 3 for different wt% of CNT and in the frequency range of 101 to 108 Hz.

Modeling based on probabilistic methods

In these methods, the distortion of carbon nanotubes and their effects are studied. The distortion which is arisen from the aspect ratio of the nanotubes in the resin causes to create more connection points compared to those created in straight nanotubes. This will change the connection resistance. Lithium and Thostenson [56] presented a probabilistic model and studied the distortion of nanotubes and the effect of this parameter on the percolation threshold and electrical conductivity. They generated a network of carbon nanotubes randomly in the form of long polygons with the equal lengths in a rectangular shape with the specified length and width and considered a random direction for each situation. They also studied the impact of aspect ratio and curvature of nanotubes. Yi et al. [57] modeled the nanotubes as sinusoidal waves in their modeling.

In Table 4, samples of theoretical (simulation, modeling) and experimental methods are provided [8, 10-19, 21, 34, 41, 42, 44, 54, 56-58]. Mendes et al. [58] used Brownian dynamics simulation for separation of the conductive and semi-conductive carbon nanotubes.

Table 1. Electrical conductivity and resistance of CNTs in theoretical method.

Researcher	Material	Chirality	Aspect ratio	Diameter (nm)	Length (μm)	Resistance ($\text{k}\Omega$)	Conductivity (s/m)	Year		
Bockrath et al.[51]	Cu	-	2	14	0 to 1000	-	1227	2008		
				22			1664			
				32			2070			
	SWCNT	Random (1/3 Metallic)	2	1	-	909 to 2857				
		All Metallic		1		2857 to 8333				
	MWCNT	-	2	14	-	175 to 8000				
				22		189 to 6250				
32				227 to 5000						
Naeemi et al.[52]	Cu	-	-	14	0.1 to 1000	-	0.1×10^4	2008		
				22			0.6×10^4			
				50			0.21×10^4			
				100			0.271×10^4			
	SWCNT		-	1	-	0.017×10^4 to 0.6×10^4				
				1.5		0.003×10^4 to 0.2×10^4				
	-----			10	-	0.006 to 0.32				
				20		0.006 to 0.6				
				50		0.006 to 1.6				
				100		0.006 to 2				
	Hosseini et al.[53]	SWCNT Bundle 27 °C	Random (1/3 Metallic)	-	2.4	10 to 80 nm length of bundle	780 to 20		-	2010
					1		475 to 10			
All Metallic			2.4		300 to 5					
1			165 to 2.5							
Copper Interconnect 27 °C		-	-	-	10 to 80 nm length of bundle	740 to 10	-			
SWCNT Bundle 100 °C		Random (1/3 Metallic)	-	2.4	10 to 80 nm length of bundle	1400 to 25	-			
				1		775 to 20				
		All Metallic		2.4		470 to 10				
		1		265 to 5						
Copper Interconnect 100 °C		-	-	-	10 to 80 nm length of bundle	760 to 20				

LITERATURE REVIEW ON EXPERIMENTAL OBSERVATIONS

Numerous researches on extracting electrical properties are devoted to the experimental methods. Experimental methods investigate parameters such as, type, geometry and structure of CNTs in isolated CNTs,

and in combination of polymer and CNT. CNT volume fraction, orientation, polymer type, method of processing, disentanglement of CNT agglomerates and CNTs connection in the solution (conductive network) are also analyzed by various investigations. The electrical conductivity, permittivity, permeability, loss

Table 2. The corresponding parameters from the equivalent circuit model.

Composite	L (H)	R1 (Ω)	C (F)	R2 (Ω)	CPE (F)	n	R3 (Ω)
m-MWCNT0.5/EP	2.03×10^{-13}	5.099	5.108×10^{-12}	4436	1.955×10^{-10}	0.9204	2.407×10^4
t-MWCNT0.5/EP	1.378×10^{-16}	3.888	1.192×10^{-11}	2.204×10^{-12}	1.202×10^{-10}	0.9653	2.397×10^4

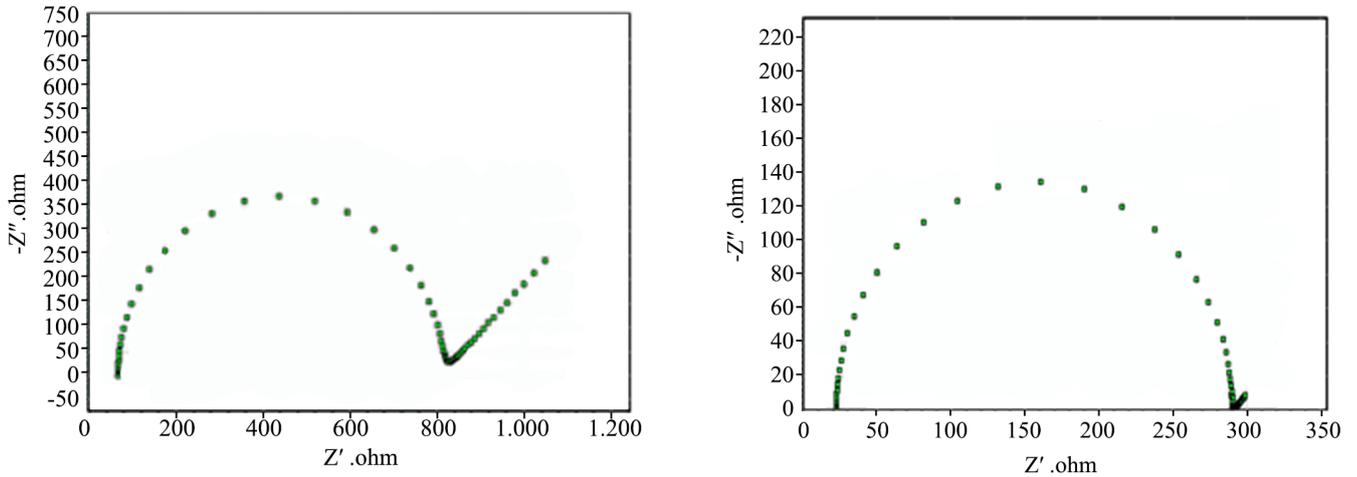


Figure 4. Impedance Nyquist plot for nanocomposites with 0.1 wt% (left) and 3 wt% (right) of CNT [55].

tangent and skin depth of CNT-reinforced polymers are investigated.

Electrical conductivity

Electrical conductivity of isolated carbon nanotubes

Among other materials, CNTs have the highest electrical conductivity [33, 59, 60] of about 109 A/cm² and 1010 A/cm² at 250°C [61]. A ballistic transport phenomenon is experienced by metallic CNTs. The traveling of metal electrons is slowed down, since they are colliding with the crystal lattice and other electrons. This process is also called scattering. The average distance which can be travelled by the electron (before scattering occurs) is called the mean free path (MFP). Finally, this process will be led to Ohm's law [62]:

$$J = \sigma E \tag{9}$$

where, J is the current density, σ the electrical conductivity and E the electric field. The electrical resistance is shown by equation 10:

$$R = l \rho / A \tag{10}$$

where l is the length (cm), A is the cross section (cm²) and ρ is the resistivity ($\Omega \cdot \text{cm}$) of the material. Finally, electrical conductivity can be obtained by reversing the resistivity, according to equation 11:

$$\rho = 1 / \sigma \tag{11}$$

Reported experimental observations in literature for the electrical conductivity of isolated carbon nanotubes [63-66] and graphenes [67] are shown in Table 5. As it can be seen from Table (5), there is as light difference between electrical conductivity of steel nanoparticles [68] as a strong conductor of electrical current and carbon nanotubes [65, 66].

In Table 6 general overview of experimental observations of DC electrical conductivity of CNT-based composites are given [8-14,21,34,63,64,75-122].

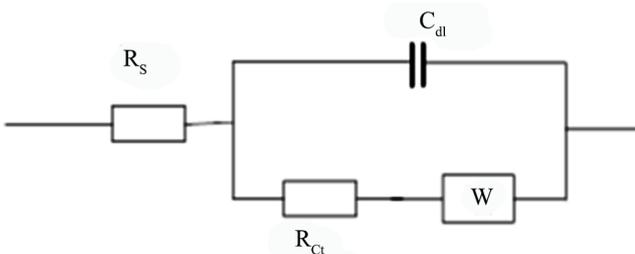


Figure 5. Electrical equivalent circuit extracted from impedance plots [55].

Table 3. Numerical values of electrical equivalent circuit elements [55].

CNTs wt%	C _{dl}	R _{ct}	R _s	Warburg coefficient
0.1	1.5 × 10 ⁻⁷	742	67	5 × 10 ⁻³
0.3	3 × 10 ⁻⁷	512	48	5 × 10 ⁻²
0.2	8 × 10 ⁻⁷	438	42	1.8 × 10 ⁻²
1	3.4 × 10 ⁻⁸	345	36	3 × 10 ⁻²
1.5	4.1 × 10 ⁻⁸	327	32	5.78 × 10 ⁻²
2	6.34 × 10 ⁻⁸	290	27	7.38 × 10 ⁻²
2.5	7.14 × 10 ⁻⁸	276	25	8.09 × 10 ⁻²
3	8.42 × 10 ⁻⁸	268	22	9.12 × 10 ⁻²

Table 4. Evaluation methods of electrical properties of isolated carbon nanotubes and nanocomposites containing CNTs.

Researcher	Method	Experimental	Theoretical					
			Theory	Electrical circuit modeling		modeling	Brownian dynamics simulations (BDS)	
				isolated CNT	CNT-based composite (Semi empirical)			Probabilistic method
				SWCNT				
[10-15, 34]								
[8, 15, 21, 34, 44]								
[41, 42, 44]								
[16-19, 54]								
[56, 57]								
[58]								

Electrical conductivity of CNT-based composites

Electrical conductivity of CNT-based composites in both DC and AC are presented in Tables 5 and 6, respectively.

A) Direct current electrical conductivity

The majority of investigations are carried out on DC electrical conductivity.

Mamunya et al. [69] in their recent research achieved the electrical conductivity about 1000 S/m and percolation threshold of about 0.396 wt% for the nanocomposite samples. Also Liao et al. [70] achieved the electrical conductivity about 0.75×10^5 S/m in the metallic nanocomposite where vinyl ester resin was used with 70 wt% graphite and MWCNTs loadings up to 2 phr. Their results showed that increasing the CNT loading up to 1 phr led to the increase in the electrical conductivity and after that it remained almost constant.

Yan et al. [71] investigated effects of length, diameter, concentration, and interface properties of CNT-based composite using the average field theory. When the aspect ratio (M) was greater than 15, the percolation threshold (f_c) of the CNT composite was inversely proportional to the CNT aspect ratio [72], i.e., $f_c = 0.7/M = 0.7d/L$, which was found by Monte Carlo

simulation [73–74].

Researchers achieved the DC electrical conductivity of CNT/PMMA composites about 1000 S/m [79], 3000 S/m [78] and 10000 S/m [14]. In some cases, the electrical conductivity increased 10 orders of magnitude higher than that for pure polymer. The level of electrical conductivity for PMMA polymers is about 10^{-7} S/m. Kim et al. [78] obtained 3×10^3 S/m electrical conductivity of composite by adding less than 0.4 MWCNT to PMMA. On the other hand, Skakalova et al. [14] with the higher volume fraction of SWCNT reached to higher electrical conductivity, compared to the work of Kim et al. [78] that used MWCNT in fabrication of nanocomposite. Also Grimes et al. [21] used PMMA with 2×10^{-10} S/m and SWCNT with 3×10^4 S/m electrical conductivities and achieved the composite with electrical conductivity of about 0.4 with using in-situ polymerization method, which was comparable with the work of Kim et al. [78,79].

The electrical conductivity of nanocomposite containing the insulated polymers such as PMMA and PS [108] with DC electrical conductivity 10000 S/m showed that the highest value of electrical conductivity of nanocomposites was independent of the conductivity of polymers, but ultimately could not be neglected the effects of conductive polymers such as PANI with 3000 S/m [102] and PPY with 4000 S/m [120] in increasing the total electrical conductivity. In more nanocomposites samples with high electrical conductivity, such as [21] with 0.4 S/m, [100] with 200 S/m, [64] with 398 S/m, [104] with 1600 S/m, [117] with 5100 S/m and [120] with an electrical conductivity about 9100 S/m, in-situ polymerization method

Table 5. Electrical conductivity of isolated carbon nanotubes.

Researcher	CNT type	Electrical conductivity (S/m)
Grimes et al. [21]	SWCNTs	3×10^4
Sundaray et al. [63]	MWCNTs	10^4
WU et al. [64]	MWCNTs	2×10^4
Kim et al. [65]	CNT	10^5
Ma et al. [66]	SWCNT	10^4 to 10^6
Kuilla et al. [67]	MWCNT	10^5 to 10^7
Lewandowska et al. [68]	Graphene	7200
	Nano sized steel	1.35×10^6

Table 6. DC electrical conductivity of CNT-based composites.

Researcher	Matrix	CNT type	CNT weight fraction (wt%)	Method of Processing	Matrix electrical conductivity (S/m)	Composite electrical conductivity (S/m)	f_c (wt%) t
Liu et al. [8]	PU	SWCNT (modified arcing method)	2	Solution	–	2.2×10^{-2}	~0.2
Saini et al. [9]	PS	PANI-MWCNT (CVD)	10 to 30	In-situ oxidative polymerization route	$\approx 10^{-16}$	5.4×10^{-3} to 3.5	0.5
Martin et al. [10]	Epoxy	MWCNT (CVD) d=50, l=43 ±3	0.01	In-situ polymerization	–	10^{-3}	– 8.6×10 ²
Sandler et al. [11]	Epoxy	MWCNT (CVD) d=50, l=17±3	1	In-situ polymerization	$\approx 10^{-9}$	2	2.5×10^4 1.2
Moisala et al. [12]	Epoxy	MWCNT	0.5	Experimental	–	4×10^{-1}	–
Kim et al. [13]	PC	MWCNT	5	Experimental	–	6.4×10^1	–
Skakalova et al. [14]	PMMA	SWCNT(HiPCO)	10	Experimental	–	10^4	–
Grimes et al. [21]	PEMA	SWCNT arc-discharge	≤23	In-situ polymerization	$\approx 2 \times 10^{-10}$	≈0.4	≈3
Logakis et al. [34]	PET	MWCNT d= 9.5, l= 1	2.5	In-situ polymerization	–	3×10^{-1}	6×10^{-2}
Sundaray et al. [63]	PMMA	MWCNT	<2	Electrospinning	10^{-12}	5.3×10^{-2}	< 5×10^{-2} –
Wu et al. [64]	PPY	MWCNT (CVD)	≤3	In-situ chemical oxidative polymerization	1.56×10^2	≈ 3.98×10^2	–
Benoit et al. [75]	PMMA	SWCNT	≤8	Solution mixing	$\approx 5 \times 10^{-6}$	≈ 7×10^1 (8 wt%)	3.3×10^{-1} 2.1
Stephan et al. [76]	PMMA	MWCNT	≤16	Spin coating	$\approx 5 \times 10^{-11}$	10^{-3} (16 wt%)	≈0.5 –
Fischer et al. [77]	PMMA	SWCNT(HiPco)	≤7	Coagulation method	$\approx 10^{-9}$	≈ 1×10^{-2} (7 wt%)	≈1 –
Kim et al. [78]	PMMA	MWCNT(CVD)	≤0.4	Solution mixing	< 10^{-7}	≈ 3×10^3 (0.4 wt%)	3×10^{-3} 2.15
Kim et al. [79]	PMMA	MWCNT (CVD)	≤40	Solution mixing/ casting	10^{-7} (0.001 wt%)	10^3 (0.3 wt%)	≈ 3×10^{-3} –
Chauvet et al. [80]	PMMA	SWCNT (arc discharge)	10.4	Solution mixing/ casting	–	≈ 5×10^1 (10.4 wt%)	4.29×10^{-1} 2.1
Du et al. [81]	PMMA	Purified SWCNT (HiPco)	≤2	Coagulation method	–	≈ 5×10^{-3}	3.9×10^{-1} 2.3
Pötschke et al. [82]	PC	MWCNT d=10-15, l=1-10	≤5	Melt mixing	$\approx 10^{-14}$	≈1 S/m (5 wt%)	1.44 t = 2.1
Ramasubramaniam et al. [83]	PC	PPE: SWCNT (HiPco)	7	Solution mixing	10^{-13}	4.8×10^2	5×10^{-2} - 10^{-1}
	PS	SWCNT-functional		Experimental	–	6.89	4.5×10^{-2}
Pötschke et al. [84]	PC	MWCNT (CVD)	3	Extruded	–	5	1 3.8
Pötschke et al. [85]	PC	MWCNT	≤15	Melt extrusion	$\approx 10^{-13}$	≈10	1–1.5
Pötschke et al. [86]	PC	MWCNT	≤15	Melt mixing	≈ 2×10^{-13}	≈ 1×10^3	1–1.5
Pötschke et al. [87]	PC	MWCNT (CVD) d=10-15, l=1-10	15	Experimental	–	10	1–2
Kim et al. [88]	Epoxy	SWCNT	≤0.21	High frequency sonication	–	≈ 1.25×10^{-3}	7.4×10^{-2}

Song et al. [89]	Epoxy	MWCNT(CVD)	≤ 1.5	Solution mixing $d=20, l=10-50$	$\approx 10^{-7}$	≈ 0.5	5×10^{-1}
Barrau et al. [90]	Epoxy	SWCNTs/DWCNTs	≤ 0.4	Solution mixing	10^{-13}	$\approx 10^{-2}$ (0.4 wt%)	8×10^{-2} 2.28
Gojny et al. [91]	Epoxy	MWCNT	≤ 0.5	Calendering process	$\approx 10^{-8}$	$\approx 10^{-2}$ (0.5 wt%)	$< 10^{-1}$ –
Thostenson et al. [92]	Epoxy	MWCNT $d=15$ to $20, l > 10$	≤ 5 wt%	Calendering process	$\approx 10^{-15}$	$\approx 5 \times 10$ (5 wt%)	$< 10^{-1}$ –
Wu et al. [93]	Epoxy	MWCNT(CVD) $d=20, l=\text{several}$ microns	23.1	Experimental		0.1 In 1 GHz (AC)	–
Huang et al. [94]	Epoxy	SWCNT (Modified arc- discharge)	15	In-situ polymerization	2.44×10^{-11}	2×10^1	6.2×10^{-2} 2.68
						4	3.18×10^{-1} 2.22
Kovacs et al. [95]	Epoxy	MWCNT (CCVD) $d_{in}=4, d_{out}=15$ $l=15$	1	In-situ polymerization	10^{-9}	4×10^{-1}	1.1×10^{-2} 1.7
Yu et al. [96]	Epoxy	SWCNT (Arc), Carbon Solutions Inc.	4	Sonicated, stirred		10	4×10^{-2} 1.7
Liu et al. [97]	Epoxy	SWCNT (Arc)	14	Manually mixed		10^{-2}	6×10^{-1}
Li et al. [98]	Epoxy	MWCNT (CVD)	1	Sonicated		2×10^{-2}	2.7×10^{-1}
Deng et al. [99]	PANI	MWCNTs	≤ 10	In-situ emulsion polymerization	2.6×10^{-1}	6.6	–
Long et al. [100]	PANI	MWCNTs	—	In-situ chemical oxidative polymerization	1.1	$\approx 1.27 \times 10^2$	< 24.8
Sharma et al. [101]	PANI	MWCNTs	30	solution casting	–	2.6×10^{-4}	–
			50			1.7×10^{-1}	
Blanchet et al. [102]	PANI	SWCNT	15	Sonicated		3×10^3	3×10^{-1} 2.1
Dalmas et al. [103]	SBA	Purified MWCNTs	≤ 5.4	Suspension mixing	$\approx 10^{-11}$	≈ 20	–
Kymakis et al. [104]	PPY	CNTs	≈ 50	In-situ polymerization	3×10^2	$\approx 1.6 \times 10^3$	–
Koerner et al. [105]	PU	MWCNT	10 vol%–0.5	solution casting		10^2-10^3	5×10^{-3}
Gryshchuk et al. [106]	VE	MWCNT (CVD)	2	Sonicated, stirred		4×10^{-2}	$< 5 \times 10^{-1}$
Battisti et al. [107]	UP	MWCNT	0.3	Experimental	–	1.3×10^{-1}	2.6×10^{-2}
Grossiord et al. [108]	PS	MWCNT (thermal CVD)	2	Experimental		10^3	1.5×10^{-1} - 2×10^{-1}
Poa et al. [109]	PS	MWCNT (Arc)	25	Sonicated, hot pressed		3×10^2	< 12
Li et al. [110]	PVA	MWNT	60	Experimental		100	5–10
Yoshino et al. [111]	PAT	MWCNT (CVD)	35	Sonicated		5×10^1	12 2.6
Saeed et al. [112]	PCL	MWCNT (CVD) $d=10-20, l=10-50$	7	Sonicated, stirred		10	1.5
Mitchell et al. [113]	PCL	SWCNT	3	Sonicated		10^{-3}	0.09 1.5
Mierczynska et al. [114]	PE, UHMW	MWCNT (CVD)	1	Sonicated, dry mixed, hot pressed		5×10^1	0.045 2.6
Lisunova et al. [115]	PE, UHMW	MWCNT (CVD)	0.7	stirred		10^{-1}	0.14 1.8

Zhao et al. [116]	PVDF	MWCNT (CVD) d= 10–50, l= 4 to 10	2	In-situpolymerization	3×10^{-10}	10	<0.07
				Sonication			
Mclachlan et al. [117]	PI	SWCNT(HiPco) d=0.9–1.2, l=3	-	Shear	6.3×10^{-15}	8.9×10^3	5×10^{-4}
				Sonication		3.2×10^2	5.06×10^{-4}
				In-situ polymerization		5.1×10^3	5.55×10^{-4}
Kilbride et al. [118]	PVA	SWCNT	-	Sonication spin casting	$\approx 10^{-10}$	2×10^{-3}	2.9×10^{-4}
Barrau et al. [119]	Epoxy	SWCNT	-	Shear in-situ polymerization	$\approx 10^{-14}$	7×10^{-2}	3×10^{-3}
Wu et al. [120]	PPY	MWCNTs	1	In-situ chemical oxidation polymerization		40×10^2	
						With coating 0.5 % PSS/ pyrrole monomer 91×10^2	
Li et al. [121]	PEDOT: PSS	MWCNT	0	spin coating		2.80	
			0.2			9.16	
Hermant et al. [122]	PEDOT: PSS	SWCNTs (HiPCO)	2.2	In-situ reduction		100	0.32
Gryshchuk et al. [123]	VE	MWCNTs (CVD)	0.5	sonication	10^{-10}	1.94×10^{-4}	---
	VE		1			2.94×10^{-2}	
	VE		2			4.05×10^{-2}	
	VEUH		0.5			1.30×10^{-4}	
	VE/EP		0.5			3.84×10^{-2}	
Wang et al. [125]	Epoxy	SWCNTs	0.5-7	solution casting	---	9×10^{-11} - 1.5×10^{-6}	---
Shafi Ullah Khan[126]	Epoxy	MWCNTs	0.05 Random 0.05 Parrallel to alignment 0.05 Prependicular to alignment	sonication	---	10^{-7}	---
						10^{-5}	
						10^{-6}	

has been used for fabrication. As it can be understood from Table 6, the percolation threshold of CNT/epoxy has been reported from 0.0025 wt% to 1 w% based on the CNT type and fabrication process.

The use of CNTs with high aspect ratios have led to a good dispersion of CNT in polymers at low concentration. This subject has been studied by Thosten et al. [124]. Recent studies show that the electrical properties of CNT-based composites depends strongly on factors such as polymer matrix, method of processing, types of CNT and especially CNT alignment[125,126]. Through aligning CNTs, Khan et al. [126] achieved electrical conductivities from 10^{-7} S/m

for composites with random orientation CNTs inside the polymer to 10^{-5} S/m for the CNT/polymer nanocomposites with parallel orientation CNTs aligned into the polymer. Different results on the CNT-based composites originated from different employed materials and measurement techniques are reported.

B) Alternative current electrical conductivity

An overview of experimental studies on AC electrical conductivity of CNT-based composites is presented in Table 7 [10, 34, 55, 65, 117, 127,128].

We investigated the real part of complex electrical conductivity in frequency range of 10^{-2} - 10^6 Hz at room

temperature (Table 7). In all nanocomposite samples the phase lag between the measured impedance and AC voltage used at low frequencies was negligible. So, the impedance at 0.01 Hz frequency was equal to the direct current (dc) resistance and the percolation threshold was reported to be about at this frequency.

According to equation 1, the AC electrical conductivity is directly related to the permittivity and frequency, and increases by increasing them [6]. Zhi Hua et al. [127] investigated that by increasing frequency from 0.3 to 18 GHz, both the real and imaginary parts of AC electrical conductivity are increased, but the increase in the electrical conductivity by increased frequency, does not have any practical benefit.

In the research done by Slepian et al. [129], the properties of CNT-based composites in the terahertz frequency range were studied. They had compared the results obtained from the theoretical study with the experimental observations, and reported a slight difference in a wide range of frequency and temperature.

AC electrical conductivity and complex permittivity can be calculated using equation 12:

$$Z^* = \frac{U^*}{I^*} \quad (12)$$

Permittivity of CNT-based films and composites

CNT films have outstanding electromagnetic properties. For example, well aligned CNT films have an effective and reduced complex permittivity function [130]. Several articles have studied the complex permittivity of different types of carbon nanotubes at low frequencies (upto1GHz). The experimental results on the permittivity of CNT-based composites are shown in Table 8. Wu et al. [93] reported the extreme dependence of the permittivity on the concentration of CNTs in the polymer matrix. In general, the permittivity of homogeneous and isotropic materials is a function of frequency and temperature [131,132]. Complex permittivity of MWCNT composites is extracted as a function of frequency [133].

Watts et al. [134] found that the real part of complex permittivity of defective CNTs in polystyrene films was higher than that of graphite nanotubes at X-band frequency. Grimes et al. [135] fabricated the SWCNTs-based composite with dimensions of about $2 \times 5 \times 0.5$ (mm) using the SWCNTs with aspect ratio

about 100. It was observed that the dielectric response was very sensitive to the concentration of metallic CNTs and the permittivity of about 100 was achieved. Both theoretical and experimental methods imply that the percolation threshold strongly depends on the aspect ratio and filler particles [136, 137].

Wu et al. [93] studies showed an extremely dependence of real and imaginary parts of relative permittivity on the frequency and concentration of CNTs in the polymer matrix. They prepared samples through addition of MWCNTs between 0.5 to 25.9 volume fraction in an epoxy polymer in frequency range of 10 MHz to 20 GHz, and found that both parts of relative permittivity at megahertz frequency were very high but at gigahertz frequency they showed extremely low values.

The results of experimental studies performed on the permittivity of CNT-based composite are given in Table 8 [7-9,21,55,65,93,94,101,127,133,134,138-146].

Both real and imaginary parts of complex relative permittivity of CNT-based composites are functions of frequency. At low frequencies, the permittivity of CNT-based composites is very high. Grimes et al. [21] with SWCNT/PEMA composites in frequency range between 0.5 to 5.5 GHz with 23% CNT weight fraction reached to the permittivity with real and imaginary parts of between 135 to -27 and 300 to 40, respectively. Also, for MWCNT/PVDF composites having 1% CNT weight fraction in frequency range between 0.1×10^{-6} to 1×10^{-3} Hz, Ghallabi et al. [147] obtained the permittivity with the real part of about 3700 to 6500 at 20°C. For having a nanocomposite with high electrical properties, a low permittivity, especially in its imaginary part, is needed. In most of nanocomposites the imaginary part of permittivity is smaller than its real part [8, 94, 134, 143]. Whereas, according to equation 6, the increase of the loss factor (imaginary part of permittivity ϵ) of nanocomposites leads to materials with high absorption properties. Nanocomposites with high absorption properties are not suitable for use in electromagnetic waves reflector structures. Although, Huang et al. [94] showed that the imaginary part of permittivity could be higher than its real part for a high content of SWCNT (15 wt%) in epoxy resin in frequency range between 8.2 to 12.4 GHz. Also, they found that $\tan(\delta)=1.42$, a more appropriate value compared to that for other samples of nanocomposites.

Table 7. AC electrical conductivity of CNT-based composites.

Researcher	Matrix	CNT type	CNT weight fraction (wt%)	method of Processing	Frequency	Composite complex conductivity (S/m)		Year
						real	imaginary	
Martin et al. [10]	Epoxy	MWCNTs (CVD) d=50 nm, l=43±3 μm l/d=340	0.01	In-situ polymerization	1 to 10 ⁵ Hz	2.5 × 10 ⁻⁹ to 5 × 10 ⁻⁵ (room temperature)		2004
						3 × 10 ⁻⁴ (80°C)		
						3 × 10 ⁻³ (140°C)		
Logakis et al. [34]	PET	MWCNT	0	In-situ polymerization	10 ⁻¹ to 10 ⁶ (Hz)	6 × 10 ⁻¹² to 8 × 10 ⁻¹³		2010
			0.5			8 × 10 ⁻³ to 1 × 10 ⁻²		
			2.5			6 × 10 ⁻¹		
Kim et al. [65]	PDDA	MWCNT	0	---	10 ⁻³ to 1.8	2 × 10 ⁻⁴ to 3 × 10 ⁻¹		2006
			0.5			4 × 10 ⁻⁴ to 3.5 × 10 ⁻¹		
			1			9 × 10 ⁻⁴ to 6 × 10 ⁻¹		
			2			5 × 10 ⁻³ to 8 × 10 ⁻¹		
			3			2 × 10 ⁻² to 1		
			4			1 × 10 ⁻² to 0.5		
			5			3 × 10 ⁻² to 1		
			8			2.5 to 10		
Mclachlan et al. [117]	PI	SWCNT (HiPco) d= 0.9–1.2 l= ~3	0	In-situ polymerization	10 ⁻² to 10 ⁶ Hz	~0.5 × 10 ⁻¹⁵ to × 10 ⁻⁷		2005
			0.5			~2 × 10 ⁻⁵ to 8 × 10 ⁻⁵		
			1			~2 × 10 ⁻⁴		
			2			~10 ⁻³		
			5			~5 × 10 ⁻³		
ZhiHua et al. [127]	PEMA	SWCNT	4	Theoretically	3 × 10 ⁻¹ to 18 GHz	1.08 × 10 ⁻¹ to 5.50	8.1 × 10 ⁻² to 4.11	2008
			8			< 1.25 to 5.25	< 1.25 to 6.6	
			10			< 1.25 to 5.90	< 1.25 to 7.2	
			13			< 1.25 to 7.12	< 1.25 to 8.15	
Barrau et al. [128]	Epoxy	MWCNT	2.5	In-situ polymerization	10 ⁻² to 10 ⁶ Hz	1 × 10 ⁻²		2003
Rafiee et al. [55]	EP/VE	MWCNT (CVD)	0.3	In-situ polymerization	12.4 to 18 GHz	1.99 to 2.2		2014
			0.5			2.27 to 2.7		
			1			2.62 to 3.1		
			1.5			3.65 to 4.7		
			2			4.14 to 5.5		
			2.5			6.2 to 8.6		
			3			8.27 to 11.3		

In the samples having 3% volume fraction of CNTs fabricated by Liu et al. [138] at frequency of 1 GHz, the real and imaginary parts of relative permittivity improved with change in the types of CNTs (single, double and multi-walled) and diameter. For the mixture of silicone and toluene with SWCNTs with diameters between 1 to 2 nm, they reported the values of 16 and 18, respectively, for the imaginary and real parts of permittivity. The imaginary and real parts of permittivity for DWCNTs with diameters between 2 to 4

nm, were 33 and 32 and for MWCNTs with diameters between 8 to 15 nm, were 400 and 360, respectively. According to equation 6, the loss tangents of these samples were found to be 0.571, 1.031 and 1.111, respectively. Also, the dielectric dissipation factor for the sample with combination of the CNTs/epoxy was reported to be 0.44 to 0.45 [144].

The loss tangent for the MWCNTs/PVC nanocomposite having 5% volume fraction of MWCNT at frequency 12.4 GHz was reported to be about 0.071

Table 8. complex relative permittivity of CNT-based composites.

Researcher	Matrix type	CNT type	Max Conductivity (S/m)	CNT weight fraction (wt%)	Method	frequency (GHz)	Complex relative permittivity		Year
							Real ($\epsilon_r, p-p$)	Imaginary ($\epsilon_i, p-p$)	
Chin et al. [7]	PVA	MWCNTs(*)	-	-	-	0.75–1.5	275 to 195	-	2011
		MWCNTs (Random)	-	-		0.75–1.5	130 to 75	-	
		MWCNTs (çç)	-	-		0.75–1.5	>60	-	
Liu et al. [8]	PU	SWCNT	2.2	0	Solution	8.2-12.4	~2	~0	2007
				5			~7	~2	
				10			~17 to 19	~9 to 11	
				15			~30 to 32	~17 to 22	
				20			32 to 38	~24 to 26	
Saini et al. [9]	PS	PANI coated MWCNT (CVD)	-	10 to 30	In-situ oxidative polymerization route	12.4 to 18.0	19 to 44	31 to 87	2011
Grimes et al. [21]	PEMA	SWCNT arc-discharge	-	0	Manually mixed	0.5 to 5.50	~2.5	~2	2007
				4			~9 to 6	~5	
				8			~20 to 10	~14 to 8	
				10 experiment			~25 to 10	~20 to 14	
				10 theory			~23 to 15	~120 to 16	
				13			~63 to 3	~105 to 38	
				15			~80 to -7	~130 to 35	
				18			~115 to -15	~205 to 40	
				23 experiment			~135 to -27	~300 to 40	
			~0.4	23 Theory			~100 to -18	~420 to 50	
Kim et al. [65]	PDDA	MWCNT (CVD)	-	0 to 8	Solution	0.001 to 1.8	3 to 440	0.1 to 2×10^4	2006
Wu et al. [93]	Epoxy	MWCNT	-	4.7	-	3 to 18	5	0.7 to 1.5	2004
				11.4			14 to 20	4 to 7.5	
Huang et al. [94]	Epoxy	SWCNT (modified arc-discharge)	-	0.5	-	8.2 to 12.4 X-band	~6	~1	2007
				1			~7.5	~3	
				3			~17 to 15	~10 to 7	
				5			~28 to 22	~19 to 14	
				10			~40 to 34	~29 to 24	
			20	15			~67 to 42	~75 to 60	
Sharma et al. [101]	PANI	CNTs	2.6×10^4	30	Solution casting	8.0–12.0	14.25 to 11.59	5.7 to 5.79	2009
		CNTs	1.7×10^1	50			39.12 to 33.34	23.47 to 25.34	
		-	-	0			3.87 to 3.25	0.52	
ZhiHua et al. [127]	PEMA	SWCNT	-	4	Theory	0.30 18	6.45 to 5.50	4.87 to 4.11	2008
				8			6.6 to 9	4.15 to 4.85	
				10			7.15 to 10.7	5.9 to 9.1	
				13			8.15 to 13.7	7.2 to 12.30	
Liu et al. [138]	Silicone and Toluene	SWCNTs	-	1	Sonication	0.001 to 1	~6 to 7	~0.2	2010
				2			~9 to 17	~0.8 to 5	
				3			~13 to 28	~1.5 to 16	
				4			~48 to 17	~46 to 2.6	
				5			~24 to 100	~6.5 to 200	

Liu et al. [138]	Silicone and Toluene	DWCNTs	-	1	Sonication	0.001 to 1	~5.4	~0.8	2010
				2			~9 to 14	~0.7 to 2	
				3			~11 to 32	~2 to 33	
				4			~18 to 95	~180 to 4.8	
				5			~20 to 130	~250 to 6	
Liu et al. [138]	Silicone and Toluene	MWCNTs	-	1	Sonication molding	0.001 to 1	~9	~0.2 to 0.3	2010
				1.5			~13 to 19	~1 to 2	
				2			~7 to 40	~2.5 to 30	
				3			~32 to 360	~17 to 400	
				4			~75 to 500	~50 to 280	
Tianjiao et al. [139]	Epoxy	MWCNTs (CVD)	-	0	-	8.2 to 17.8	~3	~0.08 to 0.11	2011
				0.5			~3.5	-	
				1			~4	~0.08 to 0.11	
				2			~5.4 to 7.8	~0.15 to 0.22	
Tianjiao et al. [142]	Epoxy	Cobalt-MWCNTs (CVD)	-	0	-	8.2 to 17.8	~2.95 to 3.03	~3.02 to 3.05	2011
				0.5			~3.02 to 3.05	~0.08 to 0.11	
				1			~3.05 to 3.13	~3.02 to 3.05	
				2			~3.18 to 3.34	~0.11 to 0.15	
Imai et al. [143]	Cellulose composite papers	MWCNT	0.05	0.5	Suspension mixing	18 to 26.5 K-band	-	-	-
			1.5	1			-	-	
			38	2.4			30 to 38	0 to 7	
			150	4.8			38 to 54	68 to 83	
			370	9.1			28 to 112	145 to 193	
			671	16.7			144 to 222	212 to 286	
Watts et al. [134]	PS	MWCNT	-	1:4 ratio films	Polymerization	8 to 12 X-band	8.5 to 9.35	0.05 to 0.18	2003
				1:4			118 to 60	0.36 to 1.1	
				1:6			45 to 17	0.5 to 1.28	
				1:8			27 to 14	0 to 0.3	
Shen et al. [140]	-	MWCNT With Iron (nanogranule)-coated	-	-	Pyrolysis of carbonyl	2	12	2.04	2005
						2 to 18	12 to 4.7	0.65 to 3.5	
Hou et al. [141]	(PVC)	MWCNTs	-	5:100	-	8.2 to 12.4	~9 to 7	~1.75 to 0.5	2012
				8:100			~10 to 7	~2 to 0	
				10:100			~10 to 13.6	~2.5 to 3.8	
				12:100			~14 to 9	~4.9 to -1.8	
Hou et al. [141]	(PVC)	Co:MWCNTs:PVC 0.2:5:100	-	Co:MWCNTs:PVC 0.2:5:100	-	~8.2 to 12.4	~5.9 to 6.9	~2.3 to 3	2012
Hou et al. [141]	(PVC)	La:MWCNTs	-	La:MWCNTs:PVC 0.2:5:100	-	~8.2 to 12.4	~12 to 10.35	~5.25 to 4	2012
Hou et al. [141]	(PVC)	Ni:MWCNTs	-	Ni:MWCNTs: PVC 0.2:5:100	-	~8.2 to 12.4	~7.3 to 5.5	~3.2 to 2.2	2012
Al Moayed et al. [146]	-	SWCNT	-	-	-	8 to 40 X, Ku, K, Ka	~80 to 20	~200 to 50	2007
Al Moayed et al. [146]	-	MWCNT	-	-	-	8 to 40 X, Ku, K, Ka	~20 to 14	~70 to 15	2007
Kim et al. [139]	Epoxy/ E-glass fibers	CNT (Thermal CVD process)	-	1	Roll milling	8.2 ~ 12.4	6.3	1.2	2010
				2			9 to 9.5	4 to 4.5	
				3			17.1 to 18.9	17.5 to 22	
				4			26.7 to 29.7	40.5 to 50	

Kim et al. [142]	Epoxy/ E-glass fibers	CNT (Thermal CVD process)	-	0.5	Roll milling	8.2 ~ 12.4	7.4 to 7.8	2 to 2.2	2010
				0.75			9 to 9.5	4.1 to 5.2	
				1			13.3 to 15.2	13.7 to 17.4	
				1.5			25.5 to 28	35.2 to 45.2	
Challa et al. [133]	Nylon 6,6 t=2.0 cm w=30 cm	MWCNT	-	1.25	Melt extrusion	8-10	5	1	2008
				2.5			9	2.5	
				5			14 to 15.5	5	
				10			25 to 27	16	
				20			47.5 to 54	58 to 75	
Zhao et al. [144]	Epoxy	MWCNT	-	10	—	8.2 ~ 12.4	13.85 to 14.87	5.85 to 6.47	2008
Han et al. [145]	—	MWCNT (CVD)	-	0	—	1 to 14	4.5 to 5.5	0 to 0.5	2011
				5.2			20 to 48	6 to 24	
				10.4			15 to 85	30 to 162.5	
Ghallabi et al. [147]	PVDF	MWCNT	-	1	Mixing and melting	0.1×10 ⁶ to 1×10 ³	1800 to 3000 in -50°C	-	2010
		Barium titanate		20			3700 to 6500 in 20°C	-	
							4650 to 9900 in 100°C	-	
							4600 to 10900 in 120°C	-	
Rafiee et al. [55]	EP/VE	MWCNT (CVD)	-	0.3	In-situ polymerization	12.4 to 18	3.9 to 3.2	2.9 to 2.2	2014
				0.5			4.3 to 3.95	3.3 to 2.7	
				1			6.3 to 5.7	3.8 to 3.1	
				1.5			7.2 to 6.8	5.3 to 4.7	
				2			8.8 to 7.4	6 to 5.5	
				2.5			11.5 to 10.5	9 to 8.6	
				3			14.6 to 13.7	12 to 11.3	

[138], for the SWCNT/epoxy nanocomposite was 0.636 [94], for the SWCNT/PEMA nanocomposite with 4% volume fraction of SWCNT was about 0.833 [62] and for the MWCNT/epoxy/E-glass fibers with 4% volume fraction of MWCNT was found to be 1.683 [139]. Grimes et al. [21] also for the SWCNT/PEMA nanocomposite with 13% volume fraction of reinforcement reported a high loss tangent about of 12.66.

In another research, by incorporation of 3 wt% of multi-walled CNTs into vinyl ester resin the real part and imaginary part of permittivity at 12.4 GHz frequency were obtained 14.6 and 12, respectively [55].

Permeability of CNT-based composites

Experimental observation on the permeability of CNT-based composites is shown in Table (9) [7, 9, 139-141, 144, 145]. Permeability can lead to a decrease in skin depth and reflection losses [9]. Chin et al. [7] obtained the real part of permeability nearly

constant and equals 1 in the frequency domain between 0.75 and 1.5 GHz, where CNTs were aligned in the electric field. The permeability of investigated materials increased, respectively, only 0.13 and 0.1 for the vertical and random arrangements of CNTs. The samples with the permeability about 1 are known as materials with non-magnetic properties.

Zhao et al. [144] reported the range of 0.06 to 0.11 for the magnetic dissipation factor ($\text{tg}\delta\mu=\mu'\mu''$) at X-band frequency.

According to the results presented in Table (9), the CNT-based composites are materials with low magnetic properties.

CONCLUSION

The influence of some factors, including CNT type (SWCNT, DWCNT and MWCNT), chirality (arm-

Table 9. complex relative permeability of CNT-based composites.

Researcher	Matrix		CNT weight fraction (wt%)	Frequency (GHz)	Complex relative permeability		Year
	Matrix type	CNT type			Real ($\epsilon_r, \mu-p$)	Imaginary ($\epsilon_r, \mu-p$)	
Chin et al. [7]	PVA	MWCNTs (^)	-	0.75–1.5	1	-	2011
	PVA	MWCNTs (Random)			1.1	-	
	PVA	MWCNTs ()			1.13	-	
Tianjiao et al. [139]	Epoxy	MWCNTs CVD	0	8.2 to 17.8	~3	~0.08 to 0.11	2011
			0.5		~3.5	-	
			1		~4	~0.08 to 0.11	
			2		~5.4 to 7.8	~0.15 to .22	
Tianjiao et al. [139]	Epoxy	Co-MWNTs CVD	0	8.2 to 17.8	~2.95 to 3.03	~3.02 to 3.05	2011
			0.5		~3.02 to 3.05	~0.08 to 0.11	
			1		~3.05 to 3.13	~3.02 to 3.05	
			2		~3.18 to 3.34	~0.11 to 0.15	
Shen et al. [140]	-	MWCNT With Iron (nanogranule)-coated	-	2	2.64	1.63	2005
Shen et al. [140]	-	MWCNT With Iron (nanogranule)- coated	-	2 to 18	2.62 to 0.75	1.62 to 0.4	2005
Hou et al. [141]	(PVC)	MWCNTs	5:100	8.2 to 12.4	~1 to 1.2	~0 to 0.2	2012
			8:100		~1.58 to 1.22	~0.05 to 0.33	
			10:100		~1.25 to 1.05	~0.1 to 0.17	
			12:100		~1.52 to 1.16	~0.15 to 0.96	
Hou et al. [141]	(PVC)	Cobalt:MWCNTs	Co:MWCNTs:PVC 0.2:5:100	~8.2 to 12.4	~1.1 to 1.25	~0.06 to 0.07	2012
Hou et al. [141]	(PVC)	La:MWCNTs	La:MWCNTs:PVC 0.2:5:100	~8.2 to 12.4	~1.46 to 0.96	~0.1 to 0.18	2012
Hou et al. [141]	(PVC)	Ni:MWCNTs	Ni:MWCNTs:PVC 0.2:5:100	~8.2 to 12.4	~1.2 to 1.4	~0.05 to 0.16	2012
Saini et al. [9]	Ps	PANI coated MWCNT (CVD)	10 to 30	12.4 to 18.0	1.01 to 1.2	0.05 to 0.6	2011
Zhao et al. [144]	Epoxy	MWCNT	10	8.2 ~ 12.4	1.02 to 1.14	0.07 to 0.11	2008
Han et al. [145]	---	MWCNT (CVD)	0	1 to 14	0.9 to 2.5	0.4 to 0.8	2011
			5.2		0.9 to 2.6	0.4 to 1.1	
			10.4		0.5 to 2.5	0.7 to 1.1	

chair, zigzag and chiral), dimension (diameter, length and aspect ratio), structure (metallic or semiconducting), method of CNTs production (CVD, arc-discharge, hipco and etc.), method of processing (solution, melt mixing and in-situ polymerization and etc.), type of polymers (insulating or conductive), volume fraction, CNTs connection in the solution (conductive network), orientation of CNTs in polymer and disentanglement of CNT agglomerates on the electrical and electromagnetic properties of CNT-based composites were discussed. Moreover, in creating the electrical circuits of the CNT-based composites some effective assumptions were considered. With these assump-

tions, however, researchers proposed equivalent circuits for SWCNTs interconnects, bundle of SWCNTs, DWCNTs and MWCNTs, but they could not offer suitable and highly precise electrical models for the CNT nanocomposites.

In contrast to the maturity of conducted simulations on mechanical behavior of CNT-based nanocomposites, a significant lack of simulation activities is identified for the specific aspect of electrical/electromagnetic behavior.

The subjects reviewed in this article indicated that in extracting the electrical properties, most of the researchers used the experimental methods, rather than

theoretical, modeling and simulation methods. Consequently, this issue is required to be further addressed in future studies.

In the majority of articles published on CNT-based composites, conductive polymers are less used to fabricate the composites. Although, a higher electrical conductivity was achieved by using insulating polymers instead of conductive polymers, studies on achieving the optimum conditions for constructing conductive CNT nanocomposites with special characteristics are still carrying out.

According to the data extracted from Tables 6-9, the CNT-based composites fabricated by applying the mentioned parameters are good replacements which can be used to make the strong structures with low weight, good conductivity and relative absorption and reflection coefficients. Finally, these materials can be employed as both electromagnetic waves absorbing and reflecting structures.

Besides, it is evident that the influence of functionalization on the electrical/electromagnetic properties of CNT nanocomposites is required to be analyzed more deeply as a challenging issue for future studies.

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